

## 5.4 What is the most entropic ideal-gas binary mixture?

For a binary mixture we have  $n_A + n_B = n$ ,  $x_A = n_A/n$ , and  $x_B = n_B/n = 1 - x_A$ . Thus Eq. (5.5) translates into

$$\begin{aligned} \Delta_{mix} S_m^{id} &= -R(x_A \ln x_A + x_B \ln x_B) = -R(x_A \ln x_A + (1 - x_A) \ln(1 - x_A)) \\ \max \Rightarrow 0 &= \frac{d}{dx_A} \Delta_{mix} S_m^{id} = -R(\ln x_A + 1 - \ln(1 - x_A) - 1) = -R \ln \left( \frac{x_A}{1 - x_A} \right) \end{aligned} \quad (5.8)$$

This is only fulfilled for  $x_A = x_B = 0.5$  which is the only maximum. This result is quite intuitive because a 50% mixture allows for the most efficient disorder of particle arrangement. Since

$$\Delta_{mix} G_m^{id} = -T \Delta_{mix} S_m^{id} \quad (5.9)$$

the minimum of the Gibbs potential is found for  $x_A = x_B = 0.5$  as well and it is more pronounced for higher temperature.