Solution to Exercise 8.1-1

Exponential Growth

- - 1. The output of the solar cell industry in 2006 2008 grew by 40 % per year. Let's assume that all solar cells installed in 2007 produced a total energy of 0.1 GW /year. Calculate (and plot) the installed power as a function of time up to 2050 for growth rates of $\alpha' = 20 \%$, 30 %, 40 %, and 50 %. What is the proper equation?
 - The general equation is $P(t) = P_0 \cdot \exp(\alpha \cdot t)$ and we know $P(t = 0 \ a) = 100 \ \text{MW}$ and $P(t = 1a) = 100 \ \text{MW} + (\alpha') = 100 \ \text{MW}$; α' is the given growth rate in %
 - It follows that

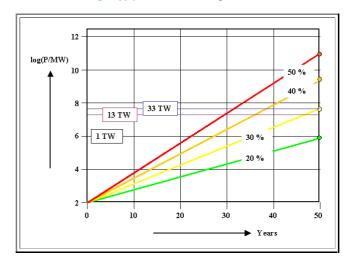
$$P(t=1a) = 100 \text{ MW} \cdot \exp(\alpha \cdot 1a \cdot a^{-1})$$

$$= 100 \text{ MW} + (\alpha'/100) \cdot 100 \text{ MW}$$

$$\alpha = \ln(1 + \alpha'/100) a^{-1}$$

$$= (0.182; 0.262; 0.336; 0.405) a^{-1}$$
for growth rates of 20%; 30%; 40%; 50%

- 2. Calculate (and plot) the installed power as a function of time up to 2050 for growth rates of 20 %, 30 %, 40 %, and 50 %.
 - That's easy and we do it, of course, in a log P(t) plot. What we get looks like this:



- **3.** What follows form the results with respect to the world-wide power scenario as described in the link??
 - It follows that with the present growth rate of 40 % all of the world's energy demands can be produced by solar cells in 35 38 years be it the <u>present</u> 13 TW or the <u>predicted</u> 33 TW
 - That looks like a "Milchmädchenrechnung" (i.e. very naive), because that's what it is. If we can sustain a growth rate of 40 % for 30 40 years remains to be seen. It's unlikely, but not impossible. The semiconductor industry, for example, sustained a growth rate of about 30 % by now for more than 35 years, and no end is in sight.

- **4.** Plot the demand for **Si**, assuming that a standard (**1000** x **1000** x **0.1**) mm³ **Si** solar cell generates **10** W on average. Will there be enough **Si**? How do the amounts of **Si** needed compare to other essential raw materials?
- The volume is $10^5 \text{ mm}^3 = 100 \text{ cm}^2$. With a density of 2.33 g/cm³ we have 23.2 g/W.
- The present (2007) production of (solar grade) Si per year is roughly 20.000 to = 2 ⋅ 10¹⁰ g; corresponding to 862 MW. If we want to produce 1 TW, we would need 23.2 ⋅ 10¹³ g = 23.2 ⋅ 10⁷ to of Si.
- That looks like a lot of Si. Yes, but look at the present world production of:
 - Iron / Steel: \approx 780 10⁶ to.
 - Coal: \approx 5 000 10⁶ to.
 - Al \approx 22 10⁶ to.
- So a few million tons of Si is definitely within present day capabilities