

## 8. Solar Cells

### 8.1 General Concerns

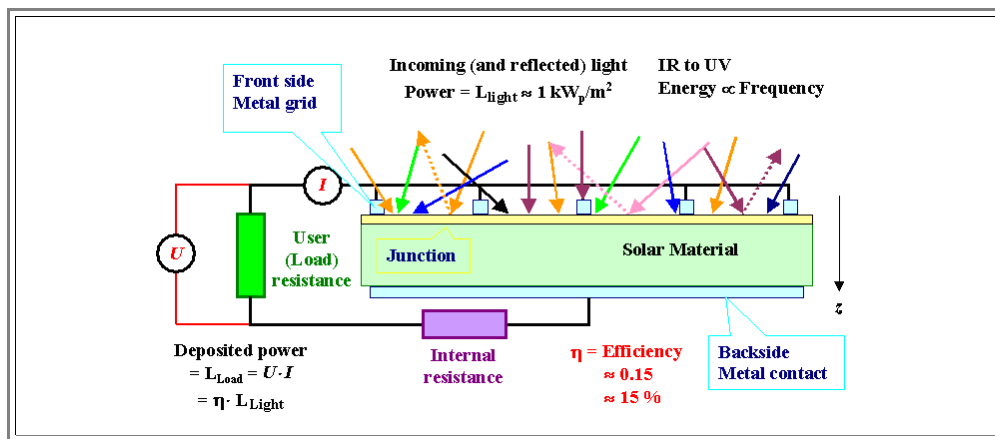
#### 8.1.1 Basic Solar Cell Topics

##### Sun, Planet, and People

- At present, *we* have to make ends meet on *our* planet called **Earth** or **Terra**, and with *our* sun, called **Sun**. In all likelihood, this will not change in the foreseeable future.
- "*We*" refers to *people* or **humans**, since it appears we are the only species on earth using energy *in excess* of what we need for just staying alive. We will see somewhat later or in this [link](#) just how much energy we need for staying alive (in a certain style).
  - What most certainly will change in the foreseeable future is *either* the way we supply ourselves with energy *or* the number of humans living (sort of) on Terra. Note that neither the planet nor the other expressions of life on Terra would give a damn about strongly declining numbers of Humans (they probably would be even very much [in favor](#) of that prospect).
- Since this Hyperscript is for that subgroup of the humans species that has a minimum of brain power *and* is willing to use it (this excludes, for example, at least one **American president**), we know that the future energy needs of humankind will have to be met by **solar energy** (in all forms: wind, "bio", solar heating, solar electricity, waves, tides, ...) and, if you like it or not, nuclear energy.
- So let's look at the most important hard facts first. They come from a host of numbers and relations, some of which are contained in the following links.
- World energy essentials:** Read the article [Future Global Energy Prosperity: The Terawatt Challenge](#) of Nobel prize winner **Richard Smalley** published in the MRS Bulletin **30, 2005**, and the article "[Powering the Planet](#)" of Nathan S. Lewis in the MRS Bulletin **32, 2007** to get a flavor of what it is all about.
  - [Solar cell essentials](#)  
This is the solar cell module from "Einführung in die Materialwissenschaft II", with which you should be thoroughly familiar.
  - [Joules, Watts and kWh's](#)  
This is a "basic" module within this Hyperscript, giving a few basic numbers and relations that you should get very well acquainted with. Your life will depend on it!
  - [Silicon for solar cells.](#)  
A module with a bit of the **30** year history around the efforts to generate cheap solar **Si**.
  - [Poly Silicon solar cells.](#)  
Some facts and stories around the "**multi crystalline**" solar cell.
  - [Some \(old\) solar cell data.](#)  
"Old" refers to the fact that solar cell research, development and production grows so fast that the above module from around **2004** is already quite outdated
  - [FAQs](#) around solar cells.  
An "advanced" module of this Hyperscript with some more information about the applicability of solar cells for energy production. It is only "advanced" because our task here is to look *only* at the technology for making solar cells: not the *application* of solar cells.
  - [Solarzellen und Materialwissenschaft](#) A German Powerpoint Presentation to the general topic

##### Solar Cell Primer

- Now let's look at the basics of solar cells as shown in the figure below.

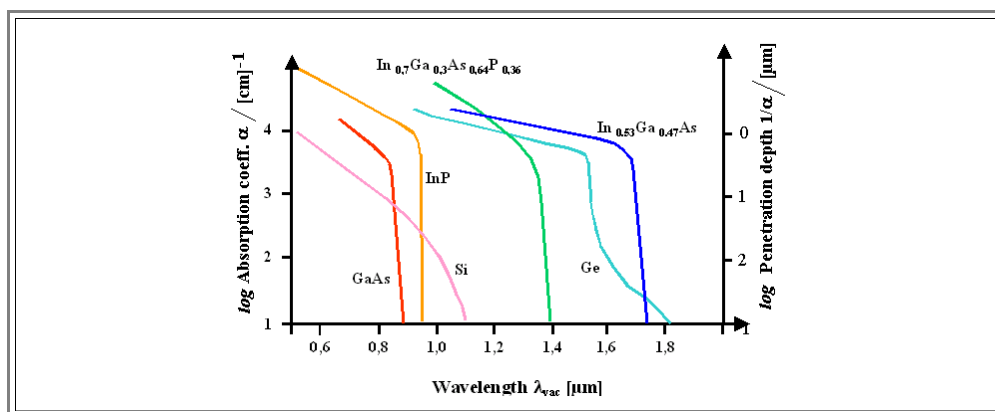


**Light:** We usually have a front side that absorbs the incoming *light* (there are a few solar cell concepts where the light can be absorbed on both sides that we will neglect here).

- The light has all kinds of frequencies according to its spectral distribution - this is pretty much a [given](#).
- It is always coming from **all directions** because there is always scattering in the air. Only if you have **direct sun light**, it will come to a large extent from *one direction*, the sun. This has an important consequence: You can focus *direct* sunlight but not indirect sunlight. Turn a large parabolic mirror into the sun and put a relatively small solar cell in its focal point and you harvest the sun energy impinging on, for example, **1 m<sup>2</sup>** in a solar cell with an area of **1 cm<sup>2</sup>**. This looks attractive in terms of saving (expensive) solar cell area but the concept is not of much use in cloudy countries like Germany. Moreover, some of the savings from needing fewer solar cells must now go to pay for all kinds of other gadgets, and you have the non-trivial problem of keeping your solar cell cool.
- A large part of the light is reflected if you just take a piece of semiconductor - after all, **Si** is shiny and [looks metallic](#) because it reflects light quite nicely. An ideal solar cell should look pitch-black - the fact that you usually can *see* solar cells proves that they are not ideal in this context. Nevertheless, any solar cell must have some anti-reflection technology on its front side; and how to do this (cheaply) is a large part of solar cell technology.
- The light with the intensity  $I_0(\delta, \nu)$  with  $\delta$ = angle of incidence and  $\nu$ = frequency at the surface, that is not lost by reflection or absorption in the grid, penetrates into the semiconductor and is absorbed according to

$$I(\delta, \nu, z) = I_0(\delta, \nu) \cdot \exp(-z/d_a)$$

- The parameter  $d_a(\delta, \nu)$  is called the **penetration depth** of the light; it can be rather large for indirect semiconductors like **Si**, e.g. **10 μm**, but also quite small - a few **nm** - depending on the semiconductor type and the frequency of the light. Obviously, only light that is absorbed inside the semiconductor can contribute to energy conversion.
- Quite often a quantity called **absorption coefficient**  $\alpha=1/d_a$  is used; the figure shows some data (for perpendicular incidence).



**Junction:** Now we have generated exactly as many electron - hole pairs as we have absorbed photons. We send some power through the load - always in the form of a simple resistor - by extracting *some* of the minority carriers produced by the light across a junction, which sweeps minority carriers that reach its **space charge region (SCR)** to the grid contact. This way we produce a **photo current density  $j_p$** = number of minorities swept to the contact per **s** and **cm<sup>2</sup>** and a **photo potential** determined by the junction potential.

- Minority carriers generated by photons that do *not* reach the junction (because, for example, they *recombine* in the bulk or at some internal surface) obviously cannot contribute to the photo-induced current density  $j_p$ . Changes for losing minorities to internal recombination grow if they have a long distance to cover (i.e. if they are produced far away from the junction) or if they find many opportunities to recombine ( $\Rightarrow$  high defect density) on their way to the junction. That's why we need "clean" **Si** for good solar cells.

- We can make a suitable junction in many ways but usually we use a **pn-junction**. [Schottky junctions](#), for example, could be (and are) used, too, but the metal part absorbs light. One kind of solar cell even relies on an electrolytic junction, but here we will not go into this.
- The current (density) - voltage  $j(U)$  relationship of an illuminated perfect **pn-junction** is described by our old **pn-junction** "master" equation

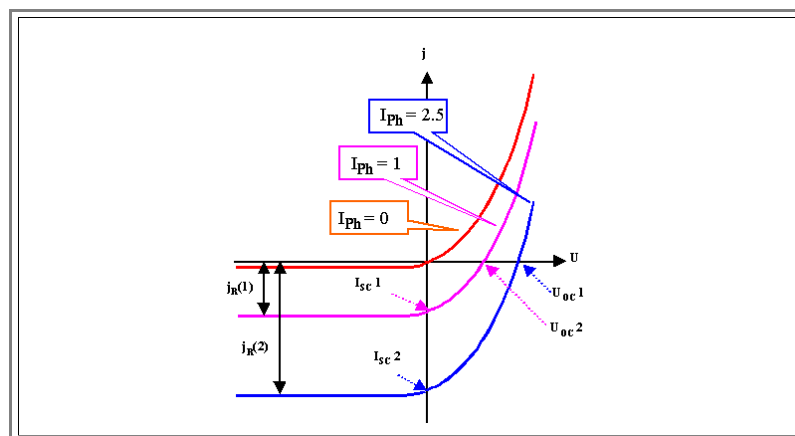
$$j = \left( \frac{e \cdot L \cdot n_i^2}{\tau \cdot N_A} + \frac{e \cdot L \cdot n_i^2}{\tau \cdot N_D} \right) \cdot \left( \exp \frac{eU}{kT} - 1 \right) + \left( \frac{e \cdot n_i \cdot d(U)}{\tau} \right) \cdot \left( \exp \frac{eU}{2kT} - 1 \right) - j_{Ph}$$

(  $j_1$  ) (  $j_2$  )

- $L$  is the [diffusion length](#) of the semiconductor,  $n_{Min}$  the minority carrier concentration ( $n_{Min} = n_i^2 / N_{dop}$ );  $n_i$  =intrinsic carrier concentration,  $N_{dop}$ = doping concentration);  $\tau$ =life time ( $\tau = L^2 / D$ );  $D$ =diffusion coefficient of carriers),  $kT$ =thermal energy,  $j_{Ph}$ =induced photo current.

▶ The two expression in front of the brackets are the reverse current densities that come from the bulk ( $j_1$ ) and the space charge region ( $j_2$ ), respectively.

- While the  $j_2$  term is often "negelcted" in text books, here we must consider the [influence of the space charge region](#) on the  $j(U)$  or, as it is often (sloppily) abbreviated, **IV** characteristics, if we want to be half-way serious about solar cells - it is the decisive term! If you activate the link you will see (once more?) that  $j_2 \gg j_1$  for **Si** and all other semiconductors with bandgap  $\gg 1$  eV.
- The resulting curves for three illumination intensities  $I_0$  (including  $I_0 = 0$ =darkness) produce characteristics with short-circuit currents proportional to the illumination intensity (or photon flux) and an upper limit of 1 carrier per photon. They look schematically like this:



- We can measure the characteristics simply by changing the load resistor  $R_{load}$  from  $R_{load} = 0 \Omega$  = **short circuit** conditions to  $R_{load} \Rightarrow \infty$  = **open circuit** condition and keeping track of the current and voltage in the external circuit.
- From these measured **IV**-characteristics we learn a lot about our solar cell; this will be treated in some detail in the next [module](#).
- Here we need to do an exercise to acquaint us again to the diode equation from [above](#) and its relevance for solar cells.

## Exercise 8 1 5

Diode equation and solar cells

- This is an important exercise! You should at least look at the solution, which will actually be given in an [advanced module](#)!

▶ **Contacts:** We need electrical contacts to the front and back of the solar cell in order connect our *constant current source* "solar cell" with the load.

- On the front side this is either done by a **grid** of metal contacts, which then always absorbs some of the incoming light without generating power, or by a layer of some transparent conductor, which then will lead to problems with the resistivity.
- At this point we finally must realize that solar cell technology is the art of making **compromises** - you can never get one parameter at the best possible value without compromising others. This is true for purely technical parameters like in the task metioned above (find the best compromise between series resistance *and* the area needed for contacts), but in particular for all tasks where one of the parameters is **money**=costs.

- An always unavoidable internal **series resistance**  $R_{SE}$  is switched in series to the load and "eats up" a part of the voltage generated according to  $U_S = R_{SE} \cdot I$  and thus reduces the efficiency.

**Load:** We have a load that "consumes" the power provided.

- The power provided by the solar cell in the external load (symbolized by a load resistor  $R_{load}$ ) is simply given by  $U_{load} \cdot I_{load}$ .
- The current flowing through  $R_{load}$  is the same as the current  $I_{SC}$  ( $=I$  in the characteristics) flowing through the solar cell, but  $U_{load} \cdot I_{load}$  is smaller than the voltage  $U_{SC}$  of the solar cell ( $=U$  (or  $V$ ) in the characteristics) by the voltage drop in the serial resistor  $R_{SE}$ , i.e.  $U_{load} = U - R_{SE} \cdot I$ .
- Maximum power will only be delivered if the load is matched to the solar cell.  $R_{load}$  must have a value that adjusts  $U$  and  $I$  in such a way that the point of maximum power on the  $IV$  characteristics is met.
- In other words: We need some "**load management**" to always extract maximum power from our solar cell power plant. This looks more difficult than it really is; we therefore won't come back to this point again.

**Efficiency:** A solar cell is nothing but an energy transformer: Light energy goes in, electrical energy comes out. The question of efficiency then always comes up quickly.

- The relation between: input=light power to output=electrical power in the load depends on the **working point** of the solar cell, i.e. on which point exactly on the  $IV$  characteristics you run the system: solar cell plus external load.
- There is a maximum efficiency  $\eta$ , however, that obtains at the *working point of maximum efficiency*. It is easily extracted from the  $IV$ -characteristics (just multiply  $I \cdot V$  of the curve and plot it), and this maximum efficiency is meant when we talk about the *efficiency* of a solar cell.
- There is a strict theoretical limit for  $\eta$  for any given solar cell; for **Si** solar cells  $\eta \approx 25\%$  obtains. There are also practical limits; at present commercial **Si** solar cells have  $\eta \approx 15\%$ .

**Energy, Power, and Money** A solar cell exposed to sunlight produces **power = energy/time** by converting the power contained in sunlight to electrical power with an efficiency  $\eta$ .

- The power contained in the sunlight varies with the daytime, the degree of cloudiness, and the latitude. Maximum sunlight power is obtainable on a perfect cloudless day on the equator at high noon; it is around **1 000 W/m<sup>2</sup>**.
- At the latitude of Kiel (**54.12 ° N**) you have to multiply by **cos(54.12 °)=0,586**, so we get less sunlight than the people in the tropics (surprise!). But our solar cells stay cooler, and that is good for the efficiency  $\eta$ .
- When we characterize a solar cell (or a module of solar cells) in *one* number, we give its "Wattpeak"  $W_p$  nominal power, which, for a first guess, is  $W_p = \eta \cdot 1\,000\text{ W/m}^2$ . It's a little bit more complicated than that (things like "**air masses**" **AM 1.5** or **AM 1** are involved).
- The average power delivered by a solar cell, considering that the sun isn't always shining, will be about **11%** of the Peak power. **1 m<sup>2</sup>** of  $\eta=15\%$  solar cells will thus produce *per year* an amount of *energy*  $E_y = 1\,000 \cdot 0,15 \cdot 0,11 \cdot 24 \cdot 365\text{ Wh} = 145\text{ kWh}$ .
- At present rates you pay about **15 €** for this to your utility. If you count on a life time of **20** years for your solar cells, a square meter should cost no more than about **€300** to be competitive in the energy market. Of course, this kind of reckoning is naive, and the numbers have to be taken with a grain of salt, but you get the basic picture in this context. More about parts of this topic can be found in the link.

It is time for a little exercise:

## Exercise 8 1 2

Optimal Working Point of Solar Cells

### Modules

The typical **Si** solar cell - about **(12 x 12) cm<sup>2</sup>** - is not what you find on your roof: up there are solar **modules**, typically about **(1.60 x 0.8) m<sup>2</sup>** or **(1.60 x 1) m<sup>2</sup>** or any other size in the **m<sup>2</sup>** range.

- If the module contains **Si** solar cells, about **50 - 100** individual solar cells are connected (by **soldering**) in series in a "string"; several strings are connected in parallel. The series connection is absolutely necessary to raise the voltage to acceptable levels (it is far more difficult in electrical engineering to deal with large currents and small voltages than vice versa) but causes a number of [problems](#) on its own.
- If the module contains thin film solar cells, long stripes of individual solar cells, about **1 cm** wide, are connected in series in-situ, i.e. during the production process of the whole module in one fell swoop. This causes a lot of problems on its own....
- ▶ The total area of the solar cells in a module is always somewhat smaller than the module area, and the top layer of the module (usually glass) that protects the solar cells from rain, bird shit, and whatever else is in the air for a guaranteed **20** years, also reflects some of the incoming light. The efficiency of the module is therefore always somewhat smaller than the efficiency of the solar cells.
- Nevertheless, even if we count module technology under "semiconductor technology", it is not quite as challenging to solder solar cells together than to make them. It might be just as expensive, however. We will not go into this kind of module technology any more.
- But let's not kid ourselves: if you make thin film solar cells with **m<sup>2</sup>** sizes, you must switch them in series even more urgently than with bulk **Si** solar. Typically, your individual solar cell has now a size of **(7 · 1.000) mm<sup>2</sup>**, and switching these thin stripes in series must be done [in-situ](#) during manufacturing. There is no soldering involved anymore. We have a new, very complex, and very challenging facet of semiconductor technology instead.



Typical module with **9 · 6=54**  
Si bulk solar cells