## Free Electron Gas in Crystals with Unequal Dimensions

If we consider a crystal with dimensions  $L_x$ ,  $L_y$ ,  $L_z$ , it has the volume  $V = L_x \cdot L_y \cdot L_z$ .

All we have to do is to replace the periodic boundary conditions  $\psi(x + L) = \psi(x)$  by:

 $\psi(x + L_x, y, z) = \psi(x, y + L_y, z) = \psi(x, y, z + L_z) = \psi(x, y, z)$ 

This leads to simple expressions for the allowed wave vectors k.

$$k_{\rm X} = 0, \quad \pm \frac{2\pi}{L_{\rm X}}, \quad \pm \frac{4\pi}{L_{\rm X}}, \quad \dots$$

$$k_{\rm Y} = 0, \quad \pm \frac{2\pi}{L_{\rm Y}}, \quad \pm \frac{4\pi}{L_{\rm Y}}, \quad \dots$$

$$k_{\rm Z} = 0, \quad \pm \frac{2\pi}{L_{\rm Z}}, \quad \pm \frac{4\pi}{L_{\rm Z}}, \quad \dots$$

$$k_{\rm Z} = 0, \quad \pm \frac{2\pi}{L_{\rm Z}}, \quad \pm \frac{4\pi}{L_{\rm Z}}, \quad \dots$$

The pre-exponential factor, which was (1/L)<sup>3/2</sup>, now changes to (1/V) <sup>1/2</sup>.

Since all relevant quantities are usually expressed as densities, i.e. divided by *V*, and the quantization of *k* is usually given up in favor of a continuous range of *k*'s, we may just as well stick to the more simple description of a crystal with equal sides - the results are the same.