

## Exercise 2.1-2

### Derive numbers for $v_0$ , $v_D$ , $\tau$ , and $l$

Show that the claims made in the backbone text are actually true (for room temperature = **300 K**). Use the following equations taken from the backbone:

- For the [average velocity  \$v\_0\$](#)  of a particle zooming around in the crystal:

$$v_0 = \left( \frac{3k_B T}{m} \right)^{1/2}$$

- For the [mean time  \$\tau\$  between scattering](#):

$$\tau = \frac{\sigma \cdot m}{n \cdot e^2}$$

- For the [drift velocity  \$v\_D\$](#)

$$v_D = - \frac{E \cdot e \cdot \tau}{m}$$

- For the [mean free path length  \$l\$](#)  obtained for  $v_D = 0$ :

$$l = 2 \cdot v_0 \cdot \tau$$

Of course, you need numbers for the concentration  $n$  of the free carriers and for the specific conductivity  $\sigma$

- Since we are essentially considering metals, you assume for a start that you have **1** free electron per atom if you want to find a number for  $n$ . Here are a few data needed for the calculation:

Atom	Density [kg m <sup>-3</sup> ]	Atomic weight [1.66 · 10 <sup>-27</sup> kg]	Conductivity $\sigma$ [10 <sup>7</sup> $\Omega^{-1}$ m <sup>-1</sup> ]	Atomic density $n$ [m <sup>-3</sup> ] ???
<a href="#">Na</a>	970	23	2.4	
<a href="#">Cu</a>	8.920	64	5.9	
<a href="#">Au</a>	19.300	197	4.5	

You may run into some trouble with the dimensions. Just look at conversions from, e.g. **eV** to **J**, from  $\Omega$  to **V** and **A**, and at the relations between Volt, Ampere, Watts and Joule.

### Solution